# Using Microsimulation to Study Optimal Income Taxation 

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Motivation

## Policy questions looking for an answer

- Should we increase the top tax rate?
- Should we move to a flat tax system?
- Should we increase welfare benefits?
- Should we in increase in-work tax credits?
- What should be the phase-in and phase-out rate?


## Who are you gonna call?

## Who are you gonna call?

## THEY'RE HERE TO SAVE THE WORLD.



## GHESTIBUSTIERS



Mirrlees


Diamond


Saez

## Outline of the talk

- Optimal income taxation
- Theory
- Application to the Netherlands
- Revealed social preferences
- Theory
- Applications: political parties, lone parents, secondary earners
- Challenges and concluding remarks


# Optimal income taxation 

## Theory

- Given the skill distribution
- Given the elasticity of the tax base
- Given a social welfare function
- Determine the tax function that maximizes social welfare
- This was pioneered by Mirrlees (1971) for which he won the Nobel Prize in Economics in 1996


## Individuals and the government

- Individuals:
- Differ in earnings ability $n$
- Decide how much effort to supply ('hours'), which is private information, thereby choosing earnings $z(n)$
- This choice depends on the tax schedule $\tau(z)$
- Assuming for simplicity that consumption $c$ equals $z-\tau(z)$
- Government:
- Maximizes a social welfare function $\left(\int g(u(c)) f(z) d z\right)$
- Subject to a budget constraint
- Redistribution if either $u_{c c}<0$ or $g^{\prime \prime}<0$


## ABC-formula for optimal marginal tax rates

Peter Diamond, Nobel Prize in 2010, showed in his 1998 paper that under some simplifying assumptions optimal marginal tax rates are given by the ABC -formula:

$$
\frac{\tau(z)}{1-\tau(z)}=A(z) B(z) C(z)
$$

- Each income level $z$ has an optimal marginal tax rate $\tau(z)$
- The left hand side increases in $\tau(z) \rightarrow$ if something on the right goes up, $\tau(z)$ must go up
- $A(z)=\frac{1}{\varepsilon(z)}$
- $\varepsilon(z)$ is the elasticity of the tax base at $z$
- The higher the elasticity of the tax base at income $z \rightarrow$ the higher the distortion of the marginal tax rate at $z \rightarrow$ the lower the optimal marginal tax rate at $z$
- Suppose for simplicity that $A(z)$ is constant over $z$
- $B(z)=1-G(z)$
- $G(z)$ average social value of a euro for individuals above $z$
- $G(0)=1$, average social value of a euro over all people is 1
- $G(z)$ drops with income $\rightarrow B(z)$ rises with income
- $B(z)$ rises faster with Rawslian than Utilitarian SWF


Gross income $=z \longrightarrow$

- $C(z)=\frac{1-F(z)}{z f(z)}$
- $1-F(z)=$ number of individuals above $z$
- $z f(z)=$ tax base at $z$


## ... continued

- For low incomes $C(z)$ is high
- $C(z)=\frac{1-F(z)}{z f(z)}$
- $1-F(z)$ is high: still many individuals above $z$
- $z f(z)$ is low: few people $f(z)$ with low income $z$


## ... continued

- For middle incomes $C(z)$ is low
- $C(z)=\frac{1-F(z)}{z f(z)}$
- $1-F(z)$ is intermediate: still quite a lot of individuals above z
- $z f(z)$ is high: many people $f(z)$ with intermedate incomes $z$


## ... continued

- For high incomes $C(z)$ is higher again
- $C(z)=\frac{1-F(z)}{z f(z)}$
- $1-F(z)$ is lower: only few individuals above $z$
- But $z f(z)$ is lower still: very few people $f(z)$ with high income $z$
- For top incomes $C(z)$ is constant (empirical regularity)


## The C term empirically



## Combining ABC



Gross income $=z \longrightarrow$
(Jongen, 2021)

## Inputs for full optimal tax analysis for the Netherlands

- Income distribution in 2015 (Income Panel)
- With estimated Pareto-tail for the top $10 \%$
- Marginal tax rates using the tax-benefit calculator MIMOSI
- To compare with the optimum
- To recover the skill distribution from the income distribution
- Intensive margin:
- Uncompensated elasticity of 0.2 (Jongen and Stoel, 2019)
- Income elasticity of -0.05 (literature)
- Calibrated using the parameters of the utility function
- Extensive margin:
- Elasticity of 0.2 (Mastrogiacomo et al., 2017)
- Calibrated using a fixed costs of work distribution


## Effective marginal tax rates in the Netherlands



## Optimal marginal tax rates in the Netherlands



## Conclusions optimal tax analysis for the Netherlands

- There is no unique optimal income tax structure
- Flat tax rate is not optimal
- Effective marginal tax rates rather high for middle incomes
- Higher top tax rate will not generate much revenue

Revealed social preferences

## Theory

- Optimal income taxation
- Given the ability distribution
- Given the elasticity of the tax base
- Given a set of social welfare weights
- Find the tax system that maximizes social welfare
- Revealed social preferences
- Given the ability distribution
- Given the elasticity of the tax base
- Given the tax system
- Find the set of social welfare weights that makes that tax system optimal
- Pioneered by Francois Bourguignon, Olivier Bargain and Amadeo Spadaro for income taxation


## ABC-formula for optimal marginal tax rates

Starting from Diamond (1998):

$$
\frac{T^{\prime}(z(n))}{1-T^{\prime}(z(n))}=A(n) B(n) C(n)
$$

where

$$
\begin{aligned}
A(n) & =\frac{1}{\varepsilon^{1 / s}} \\
B(n) & =\frac{\int_{n}^{\bar{n}}(1-g(m)) f(m) d m}{1-F(n)} \\
C(n) & =\frac{1-F(n)}{n f(n)}
\end{aligned}
$$

## Inverting the optimality conditions

Rewriting gives

$$
\int_{n}^{\bar{n}}(1-g(m)) f(m) d m=\frac{T^{\prime}(z(n))}{1-T^{\prime}(z(n))} \varepsilon^{l^{s} n f(n) .}
$$

Taking the derivative with respect to $n$

$$
g(n)=1+\frac{T^{\prime}}{1-T^{\prime}} \varepsilon^{l s}\left(\varepsilon^{\frac{T^{\prime}}{1-T^{\prime}}}+\varepsilon^{n f}\right)
$$

where

$$
\begin{aligned}
\varepsilon^{\frac{T^{\prime}}{1-T^{\prime}}} & =\frac{\partial\left(\frac{T^{\prime}}{1-T^{\prime}}\right)}{\partial n} \frac{n}{\frac{T^{\prime}}{1-T^{\prime}}} \\
\varepsilon^{n f} & =\frac{\partial(n f(n))}{\partial n} \frac{n}{n f(n)}
\end{aligned}
$$

## Consider optimality by looking for anomalies

- Negative social welfare weights
- Social welfare weights that rise with income
- Spikes in social welfare weights


## Application 1:

## Social welfare weights political parties

(Jacobs, Jongen and Zoutman, 2017)

## Motivation


"Don't tell me what you value.
Give me your budget and I will tell you what you value!"

## Overview

- We recover the social welfare weights of the four largest political parties for the 2002 elections in the Netherlands
- Study whether social welfare weights are 'well-behaved'
- Do parties care about everybody?
- Do parties care more about the poor than the rich?
- Do left-wing parties care more about poor than right-wing p.?
- Do right-wing parties care more about rich than left-wing p.?
- Some results are in line with expectations
- But we also find some anomalies


## Effective marginal tax rates: Socialist Party (SP)

## (a) Socialist party (SP)



## Effective marginal tax rates: Socialist Party (SP)



## Effective marginal tax rates: Liberal Party (VVD)



## Social welfare weights: baseline



## Social welfare weights: Socialist Party (SP)



## Social welfare weights: Liberal Party (VVD)



## Conclusions social welfare weights political parties

- Some results are in line with expectations, grosso modo:
- All parties care more about the poor than the rich
- Left-wing parties care more about poor than right-wing parties
- Right-wing parties care more about rich than left-wing parties
- But we also uncover some anomalies
- All parties care more about middle incomes than the poor
- Left-wing parties give a negative weight to (part of) the rich
- Differences in welfare weights across parties are rather small


## Application 2:

## Income support for lone parents

(De Boer and Jongen, 2023)

## Motivation

- Lone parents are of particular interest to policymakers
- Trade-off sufficient income and sufficient incentives to work
- Major reforms in income support for lone parents in the NL
- Goals: simplify the system and improve incentive to work
- Is the new system (closer to) optimal?
- Following Blundell et al. (2009), we invert the discrete optimal-tax model of Saez (2002)


## Pre-reform income support lone parents (2006)




## Post-reform income support lone parents (2015)



## Inputs for the analysis

Table: Inputs optimal tax analysis lone parents: 2006-2009

| Gross earnings per week | Net income per week | Net tax per week | Intensive elasticity | Extensive elasticity | Share |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Panel A: Lone parents with a youngest child $0-17$ years of age ${ }^{\text {a }}$ |  |  |  |  |  |
| 0 | 293 | -293 | - |  | 0.25 |
| 200 | 314 | -114 | 0.04 | 0.04 | 0.15 |
| 326 | 384 | -58 | 0.06 | 0.13 | 0.15 |
| 423 | 441 | -18 | 0.06 | 0.16 | 0.15 |
| 544 | 503 | 41 | 0.05 | 0.20 | 0.15 |
| 851 | 659 | 192 | 0.12 | 0.35 | 0.15 |
| Panel B: Lone parents with a youngest child 0-3 years of age ${ }^{\text {b }}$ |  |  |  |  |  |
| 0 | 296 | -296 | - | - | 0.43 |
| 184 | 379 | -195 | 0.29 | 0.29 | 0.11 |
| 289 | 445 | -156 | 0.07 | 0.48 | 0.11 |
| 378 | 522 | -143 | 0.12 | 0.59 | 0.11 |
| 478 | 579 | -101 | 0.07 | 0.58 | 0.11 |
| 704 | 697 | 7 | 0.13 | 0.89 | 0.11 |

[^0]
## Social welfare weights: child 0-17 years of age



## Social welfare weights: child 0-3 years of age



## Conclusions income support lone parents

- Social welfare weights were monotonically declining in income
- Social welfare weights were sometimes negative
- The reforms mitigated these anomalies


## Application 3:

## Taxation of secondary earners

(De Boer, Jongen and Koot, 2018)

## Motivation

- Many OECD countries implemented tax-benefit reforms to promote labour participation, in particular of women
- Tax rates for secondary earners have decreased
- The Netherlands is a frontrunner
- Major reforms in the period 2005-2021
- Question: too much of a good thing?
- We again use the inverted discrete optimal-tax model of Saez (2002)


## Average tax rate dual- minus single-earner couple: 2020



## Average tax rates couples: 2005, 2017 and 2021



## Social welfare weights: child $0-17$ years



## Social welfare weights: child 0-3 years



## Optimal taxation child 0-3 years for different SWFs



## Conclusions taxation of secondary earners

- We find anomalies in the social welfare weights:
- Social welfare weights grosso modo well-behaved before reforms
- After reforms no longer monotonically declining and sometimes negative
- This suggests an imbalance between equity and efficiency
- But the optimal tax model has its limitations
- Unitary household model
- No lifecycle considerations

Challenges and concluding remarks

## Challenges for optimal tax analyses

- What is between the elasticity of hours worked and the elasticity of taxable income?
- Dealing with households/couples
- Dealing with lifecycle considerations
- Dealing with preference heterogeneity (empirically)
- Dealing with information frictions and other frictions


## Concluding remarks

- We should take up these challenges
- Make our optimal-tax models more realistic and thereby even more policy relevant
- Remain wary of the remaining limitations and how they impact your conclusions
- But a promising way to get a grip on real-life policy questions!


## Or as Darth Vader would put it



Join me and together we can rule the policy galaxy!

## Thank you!

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[^0]:    ${ }^{a} 41,339$ observations, ${ }^{b} 4,171$ observations.

